Reg. No.		
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**Question Paper Code** 

12090

### B.E. / B.Tech, - DEGREE EXAMINATIONS, APRIL / MAY 2023

Fourth Semester

### **Information Technology**

(Common to Computer Science and Engineering, Artificial Intelligence and Data Science & M.Tech. - Computer Science and Engineering)

### 20ITPC401 - DESIGN AND ANALYSIS OF ALGORITHMS

(Regulations 2020)

Duration: 3 Hours

Max. Marks: 100

# $PART - A (10 \times 2 = 20 Marks)$

Answer ALL Questions

1.	Compare the orders of growth of $n(n-1)/2$ and $n^2$ .	K-Level, CO 2,K2,CO1
2.	What do you mean by Worst case Efficiency of an algorithm?	2,K1,CO2
3.	Design a brute-force algorithm for computing the value of a polynomial $p(x) = a_n x^n + a_{n-1} x^{n-1} + \cdots + a_1 x + a0$ , where each $a_i$ is a constant.	2,K2,CO2
4.	Define Hamiltonian Circuit. Give an example.	2,K1,CO2
5.	State the principle of Optimality.	2,K1,CO3
6.	List out the memory functions used under dynamic programming.	2,K1,CO3
7.	Comment on the capacity constraint in the context of maximum flow problem.	2,K2,CO4
8.	When a linear program is said to be unbounded?	2,K2,CO4
9.	Differentiate tractable from non-tractable problems.	2,K2,CO5
10.	Depict the proof which says that a problem 'A' is no harder or no easier than problem 'B'.	2,K2,CO5

# PART - B $(5 \times 13 = 65 \text{ Marks})$

Answer ALL Questions

11. a) With suitable illustrations, explain Big Omega, Big O and Big Theta <sup>13,K2,C01</sup> Notations.

OR

- b) Give the general plan for analyzing the time efficiency of recursive 13,K2,C01 algorithms. Use recurrence to find the number of moves for Towers of Hanoi problem. Discuss its time complexity.
- 12. a) Determine the number of character comparisons made by the brute-force 13,K3,CO2 algorithm in searching for the pattern GANDHI in the text THERE\_IS\_MORE\_TO\_LIFE\_THAN\_INCREASING\_ITS\_SPEED

K1 - Remember; K2 - Understand; K3 - Apply; K4 - Analyze; K5 - Evaluate; K6 - Create

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Assume that the length of the text (47 characters long) is known before the search starts.

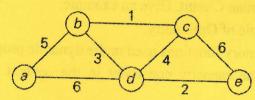
OR

- b) Devise an algorithm for Quick Sort and derive its time complexity. For 13,K3,C02 the above devised quick sort algorithm, derive the time complexity if all the elements are arranged in ascending order.
- 13. a) (i) What does dynamic programming have in common with divide-and- 3,K3,C03 conquer? What is a principal difference between them?
  - (ii) Apply the bottom-up dynamic programming algorithm to the 10,K3,CO3 following instance of the knapsack problem:

Item	Weight	Value	
1	3	\$25	
2	2	\$20	
3	1	\$15	Capacity $W = 6$ .
4	4	\$40	oupdoity ** - 0.
5	5	\$50	

OR

- b) (i) Give a counter example that shows that Dijkstra's algorithm may not 3,K3,C03 work for a weighted connected graph with negative weights.
  - (ii) Apply Kruskal's algorithm to find a minimum spanning tree of the 10,K3,CO3 following graph.



14. a) Solve the following linear programming problem. maximize x + 2y

13,K3,CO4

subject to 
$$4x \ge y$$

$$y \le 3 + x$$

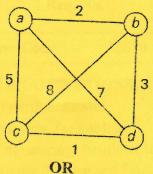
$$x \ge 0, y \ge 0$$

OR

b) Find a stable marriage matching for the instance defined by the 13,K3,C04 following ranking matrix:

	A	В	C	D
α	1,3		3, 2	
β	1,4	4, 1	3, 4	2,2
Y	2, 2	1,4	3, 3	4, 1
δ	4, 1	2, 2	3, 1	1,4

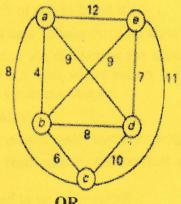
15. a) Apply the branch-and-bound algorithm to solve the traveling salesman 13,K3,CO5 problem for the following graph.



b) Apply backtracking to solve the following instance of the subset sum 13,K3,C05 problem: A =  $\{1, 3, 4, 5\}$  and d = 11.

PART - 
$$C(1 \times 15 = 15 \text{ Marks})$$

16. a) Construct a minimum spanning tree of the given graph using travelling 15,K3,C06 salesman algorithm.



b) Explain the assignment problem using a branch and bound technique 15,K3,C06 with example.