

Reg. No.

Question Paper Code

12140

14/08/2023

B.E. / B.Tech. - DEGREE EXAMINATIONS, APRIL / MAY 2023

First Semester

Computer Science and Business Systems
20BSMA102 - DISCRETE MATHEMATICS
(Regulations 2020)

Duration: 3 Hours

Max. Marks: 100

PART-A (10 × 2 = 20 Marks)

Answer ALL Questions

- | | <i>Marks,
K-Level, CO</i> |
|---|-------------------------------|
| 1. Construct the truth table for $(P \rightarrow Q) \wedge (Q \rightarrow P)$. | 2,K2,CO1 |
| 2. Write the negation of the statement $(\exists x)(\forall y)P(x,y)$. | 2,K1,CO1 |
| 3. State the Pigeonhole principle. | 2,K1,CO2 |
| 4. Find the recurrence relation of the sequence $s(n)=a^n, n \geq 1$. | 2,K2,CO2 |
| 5. State any two laws of Boolean algebra. | 2,K1,CO3 |
| 6. How many cells does a K- map in three variables have? | 2,K1,CO3 |
| 7. How many edges are there in a graph with 10 vertices each of Degree 3? | 2,K1,CO4 |
| 8. Define Hamiltonian path. | 2,K1,CO4 |
| 9. Prove that identity element in a group is unique. | 2,K2,CO5 |
| 10. Define Kernel of homomorphism. | 2,K1,CO5 |

PART - B (5 × 16 = 80 Marks)

Answer ALL Questions

- | | |
|---|-----------|
| 11. a) (i) Show that $((P \vee Q) \wedge \neg(\neg P \wedge (\neg Q \vee \neg R))) \vee (\neg P \wedge \neg Q) \vee (\neg P \wedge \neg R)$ is a tautology. | 8,K2,CO1 |
| (ii) $(P \vee Q) \wedge (\neg P \wedge (\neg P \wedge Q)) \Leftrightarrow (\neg P \wedge Q)$ using equivalence formula. | 8,K3,CO1 |
| OR | |
| b) Show that the following premises are inconsistent. | 16,K3,CO1 |
| 1. If Jack misses many classes through illness, then he fails high school. | |
| 2. If Jack fails high school, he is uneducated | |
| 3. If Jack reads a lot of books, then he is not uneducated. | |
| 4. Jack misses many classes through illness and reads a lot of books. | |
| 12. a) (i) Using induction principles prove that n^3+2n is divisible by 3. | 8,K3,CO2 |
| (ii) Using mathematical induction prove that $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$. | 8,K3,CO2 |
| OR | |
| b) Solve $S(k) - 7S(k-1) + 10S(k-2) = 8k + 6$, for $k \geq 2$, $S(0)=1$, $S(1)=2$. | 16,K3,CO2 |

K1 – Remember; K2 – Understand; K3 – Apply; K4 – Analyze; K5 – Evaluate; K6 – Create

12140

13. a) (i) In Boolean algebra, show that the following are equivalent. For any a and b , (A) $a + b = b$ (B) $a \cdot b = a$ (C) $a' + b = 1$ (D) $a \cdot b' = 0$ (E) $a \leq b$. 12,K3,CO3

(ii) In a Boolean Algebra. Show that $(a+b')(b+c')(c+a') = (a'+b)(b'+c)(c'+a)$ 4,K2,CO3

OR

- b) Find the minimal expansion as a sum of products of each of the following Boolean functions using K- map : 16,K3,CO3

(i) $f(x, y) = x y + x \bar{y}$

(ii) $f(x, y) = \bar{x} y + \bar{x} \bar{y}$

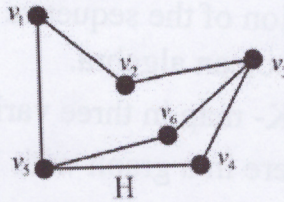
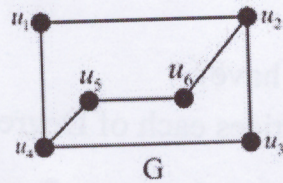
(iii) $f(x, y, z) = \bar{x} y z + \bar{x} \bar{y} \bar{z}$

(iv) $f(x, y, z) = \bar{x} y z + \bar{x} \bar{y} z$

(v) $f(x, y, z) = \bar{x} y \bar{z} + \bar{x} \bar{y} \bar{z} + x \bar{y} \bar{z} + x y z + x \bar{y} z$

14. a) (i) State and Prove Handshaking Theorem 4,K2,CO4

(ii) Examine whether the following pair of graphs are isomorphic Or not .Justify your answer. 12,K2,CO4



OR

- b) Given an example of a graph which is 16,K3,CO4
- (i) Eulerian but not Hamiltonian
 - (ii) Hamiltonian but not Eulerian
 - (iii) Both Eulerian and Hamiltonian
 - (iv) Non Eulerian and not Hamiltonian

15. a) (i) State and prove Lagrange's theorem. 8,K2,CO5

(ii) Show that the set of positive rational numbers Q^+ is an abelian group for the operation $*$ defined by $a * b = \frac{ab}{3}$. 8,K2,CO5

OR

- b) Let $(G, *)$, and $(G_1, *)$ be two groups and let $f : G \rightarrow G_1$ be a group homomorphism from G to G_1 . Prove that 16,K2,CO5

(a) $f(e) = e_1$ where e and e_1 are the identities of $(G, *)$ and $(G_1, *)$ respectively.

(b) $f(a) = [f(a)]^{-1}$ for any $a \in G$.