

16. Find the solution of $(D^2 - 5D + 6)y = 0$. 2 K2 CO2
17. Prove that an analytic function whose real part is constant must itself be a constant. 2 K2 CO3
18. Find the fixed points of the transformation $w = \frac{6z-9}{z}$. 2 K2 CO3
19. Define Essential singularity. 2 K1 CO4
20. State Cauchy's Residue theorem. 2 K1 CO4
21. Find $L[t^2 e^{-3t}]$. 2 K2 CO5
22. State the sufficient conditions for the Existence of Laplace transform. 2 K1 CO5

PART - C (6 × 11 = 66 Marks)

Answer ALL Questions

23. a) Verify Gauss Divergence theorem for $\vec{F} = (x^2 - yz)\vec{i} + (y^2 - zx)\vec{j} + (z^2 - xy)\vec{k}$ taken over the rectangular parallelepiped bounded by $x = 0, y = 0, z = 0$ and $x = a, y = b, z = c$. 11 K3 CO1
- OR**
- b) Verify Stoke's theorem for $\vec{F} = (x^2 - y^2)\vec{i} + 2xy\vec{j}$ taken round the rectangle region in the xy plane bounded by the lines $x = 0, x = a, y = 0, y = b$. 11 K3 CO1
24. a) Solve $(D^2 + 4)y = \sec 2x$ by the method of variation of parameters. 11 K3 CO2
- OR**
- b) Solve $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 4y = x^2 + \cos(\log x)$. 11 K3 CO2
25. a) Find the analytic function $f(z) = u + iv$ given that $u - v = e^x(\cos y - \sin y)$. 11 K3 CO3
- OR**
- b) Find the bilinear transformation that maps the points $z = -2, 0, 2$ into the points $w = 0, i, -i$ respectively. 11 K3 CO3
26. a) Expand $\frac{1}{z^2 - 3z + 2}$ in the region (i) $1 < |z| < 2$ and (ii) $|z| > 2$. 11 K3 CO4
- OR**
- b) Evaluate $\int_0^\infty \frac{x^2 dx}{(x^2 + a^2)(x^2 + b^2)}$, $a > 0, b > 0$ using contour integration. 11 K3 CO4
27. a) Find the Laplace transform of the periodic function $f(t) = \begin{cases} t & 0 \leq t \leq a \\ 2a - t, & a < t \leq 2a \end{cases}$ and $f(t + 2a) = f(t)$. 11 K3 CO5
- OR**
- b) Using Laplace transforms, solve $y'' + y' = t^2 + 2t, y(0) = 4, y'(0) = -2$. 11 K3 CO5
28. a) (i) Evaluate $\int_C \frac{dz}{(z+1)^2(z-2)}$, where C is the circle $|z| = \frac{3}{2}$. 6 K5 CO4
- (ii) Using convolution theorem find $L^{-1} \left[\frac{s^2}{(s^2+4)(s^2+9)} \right]$. 5 K3 CO5
- OR**
- b) (i) Evaluate $\int_C \frac{z^2}{(z-1)^2(z+2)} dz$, where C is the circle $|z| = 3$, using Cauchy's Residue Theorem. 6 K5 CO4
- (ii) Verify the initial value theorem for the function $f(t) = 3e^{-2t}$. 5 K3 CO5