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Question Paper Code	12239
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B.E. / B.Tech - DEGREE EXAMINATIONS, NOV / DEC 2023

Seventh Semester

Mechanical Engineering

(Common to Production Engineering)

20MEPC701 - FINITE ELEMENT ANALYSIS

(Regulations 2020)

Duration: 3 Hours

Max. Marks: 100

PART - A (10 × 2 = 20 Marks)

Answer ALL Questions

Marks,

K-Level, CO

2, K2, CO1

2, K1, CO1

2, K2, CO2

2, K1, CO2

2, K1, CO3

2, K2, CO3

2, K1, CO4

2, K2, CO4

2, K2, CO5

2, K2, CO5

1. Compare the Ritz technique with the nodal approximation method.
2. State the three phases of the finite element method.
3. Differentiate global and local coordinates.
4. List out the stiffness matrix properties.
5. Define plane strain analysis.
6. Write down the stress strain relationship matrix for plane stress condition.
7. What is meant by Transverse vibration?
8. Illustrate the expression of longitudinal vibration of bar element.
9. Differentiate between Isoparametric, super parametric and sub- parametric elements.
10. Give the shape functions for a four-noded linear quadrilateral element in natural coordinates.

PART - B (5 × 13 = 65 Marks)

Answer ALL Questions

11. a) Using Rayleigh-Ritz method obtain an approximate solution for the differential equation given below with boundary conditions $y(0) = 0$ and $y(1) = 0$.

13, K2, CO1

$$\frac{d^2y}{dx^2} - 10x^2 = 5 ; 0 \leq x \leq 1$$

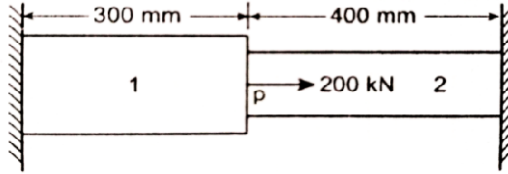
OR

- b) Solve the differential equation for a physical problem expressed as $d^2y/dx^2 + 100 = 0$, $0 \leq x \leq 10$ with boundary conditions as $y(0) = 0$ and $y(10) = 0$ using the trial function $y = a_1x(x-10)$ find the value of the parameters a_1 by the following methods listed below.

13, K2, CO1

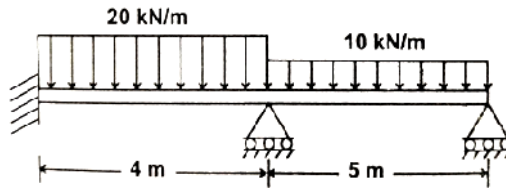
- (i) Point collocation method (ii) Sub domain collocation method (iii) Least squares method and (iv) Galerkin method.

12. a) Consider a bar as shown in figure an axial load of 200 kN is applied at a point P. Take $A_1 = 2400 \text{ mm}^2$, $E_1 = 70 \times 10^9 \text{ N/mm}^2$, $A_2 = 600 \text{ mm}^2$ and $E_2 = 200 \times 10^9 \text{ N/mm}^2$. Calculate the following (i) the nodal displacement at point P (ii) Stress in each element (iii) Reaction force. 13,K3,CO2

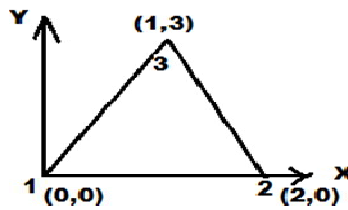


OR

- b) For the beam as shown in the fig. compute slope at the hinged support points, $E = 200 \text{ GPa}$ and $I = 4 \times 10^{-6} \text{ m}^4$. Use two beam elements. 13,K3,CO2



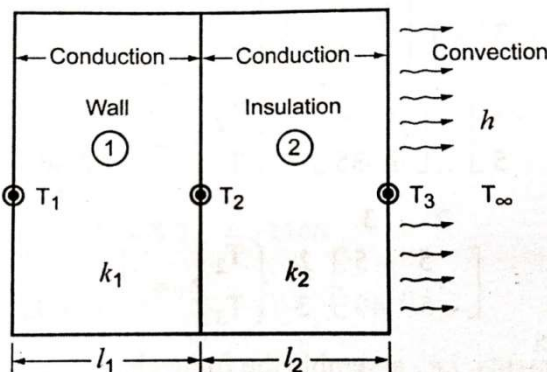
13. a) Calculate the strain displacement matrix for the CST element shown in the figure given below. 13,K3,CO3



OR

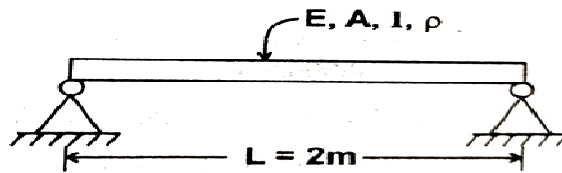
- b) Develop shape function for axisymmetric triangular elements. 13,K3,CO3

14. a) A wall of 0.6 m thickness having thermal conductivity of 1.2 W/mK. The wall is to be insulated with a material of thickness 0.06 m having an average thermal conductivity of 0.3 W/mK. The inner surface temperature is 1000°C and outside of the insulation is exposed to atmospheric air at 30°C with Heat transfer coefficient of $35 \text{ W/m}^2\text{K}$. Calculate the nodal temperatures. 13,K4,CO4

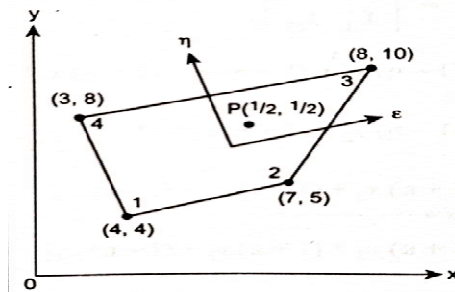


OR

- b) Find the Natural frequencies in the vibration of two elements simply supported beam having the parameters as length $L = 2\text{m}$, area of cross-section $A = 30 \times 10^{-4} \text{m}^2$ and moment of inertia $I = 4 \times 10^{-10} \text{m}^4$, density $\rho = 7800 \text{kg/m}^3$ and Young's modulus $E = 200 \text{GPa}$. 13,K4,CO4



15. a) For the four noded quadrilateral element shown in the figure. Calculate the Jacobian matrix and evaluate its value at the point $\epsilon = 0.5, \eta = 0.5$ 13,K4,CO5



OR

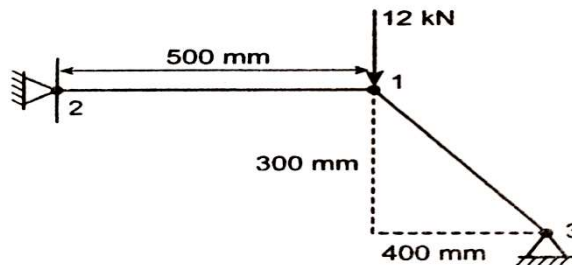
- b) Evaluate the integral, 13,K4,CO5

$$I = \int_{-1}^1 \cos \frac{\pi x}{2} dx$$

by applying 3 point Gaussian quadrature and compare with exact solution.

PART - C (1 × 15 = 15 Marks)

16. a) For the two bar truss shown in the fig, Estimate the displacements of node 1 and the stress in element 1-3. Take $E = 70 \text{GPa}$, $A = 200 \text{mm}^2$ 15,K3,CO6



OR

- b) For the plane stress CST element as shown in the fig. Calculate element stiffness matrix. Assume $E = 210 \times 10^3 \text{N/mm}^2$, $\nu = 0.25$, $t = 10\text{mm}$. The co-ordinates are given in mm. 15,K3,CO6

