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Question Paper Code	12583
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B.E. / B.Tech. - DEGREE EXAMINATIONS, APRIL / MAY 2024

Seventh Semester

Mechanical Engineering

20MEPC701 - FINITE ELEMENT ANALYSIS

Regulations - 2020

Duration: 3 Hours

Max. Marks: 100

PART - A (10 × 2 = 20 Marks)

Answer ALL Questions

- | | Marks | K-Level | CO |
|---|-------|---------|-----|
| 1. Why polynomial type interpolation functions are mostly used in FEM? | 2 | K2 | CO1 |
| 2. What is meant by discretization? | 2 | K1 | CO1 |
| 3. Define shape function. | 2 | K1 | CO2 |
| 4. Express the element stiffness matrix of a truss element. | 2 | K2 | CO2 |
| 5. Define CST element. | 2 | K1 | CO3 |
| 6. What are the required conditions for a problem assumed to be axisymmetric? | 2 | K1 | CO3 |
| 7. Define Super parametric element. | 2 | K1 | CO5 |
| 8. Give the shape functions for a four-noded linear quadrilateral element in natural coordinates. | 2 | K2 | CO5 |
| 9. What is meant by Longitudinal vibration? | 2 | K1 | CO6 |
| 10. Define Heat Transfer. | 2 | K1 | CO6 |

PART - B (5 × 13 = 65 Marks)

Answer ALL Questions

- | | | | |
|--|----|----|-----|
| 11. a) Describe the step by step procedure of solving FEA. | 13 | K2 | CO1 |
| OR | | | |
| b) Solve the differential equation for a physical problem expressed as | 13 | K2 | CO1 |

$$d^2y/dx^2 + 50 = 0, 0 \leq x \leq 10$$

with boundary conditions as $y(0)=0$ and $y(10)=0$ using (i) Point collocation method (ii) Sub domain collocation method (iii) Least square method and (iv) Galerkin method

- | | | | |
|--|----|----|-----|
| 12. a) For a tapered bar of uniform thickness $t = 10\text{mm}$ as shown in figure-1. Predict the displacements at the nodes by forming into two element model. The bar has a mass density $\rho = 7800 \text{ kg/m}^3$, the young's modulus $E = 2 \times 10^5 \text{ MN/m}^2$. In addition to self-weight, the bar is subjected to a point load $P = 1 \text{ kN}$ at its Centre. Also determine the | 13 | K3 | CO2 |
|--|----|----|-----|

K1 – Remember; K2 – Understand; K3 – Apply; K4 – Analyze; K5 – Evaluate; K6 – Create

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reaction forces at the support.

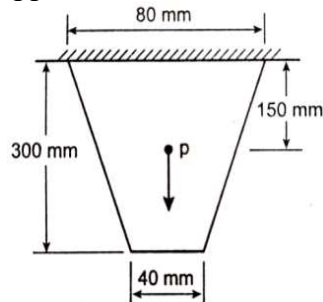


Figure-1

OR

- b) Derive the displacement function u and shape function N for one dimensional Linear bar element based on global co-ordinate approach 13 K3 CO2

13. a) Derive the shape function for CST elements. 13 K3 CO3

OR

- b) Calculate the element stiffness matrix for the axisymmetric triangular element shown in fig-2. The coordinate are in mm. Take $E=2 \times 10^5$ N/mm², $\nu = 0.25$. 13 K3 CO3

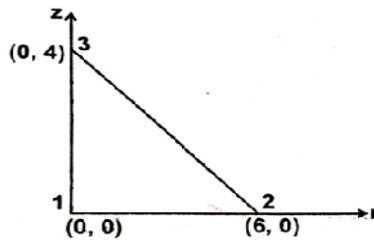


Figure-2.

14. a) For a four noded rectangular element shown in fig-3. Estimate the following (i). Jacobian matrix (ii). Strain-Displacement matrix 13 K3 CO5

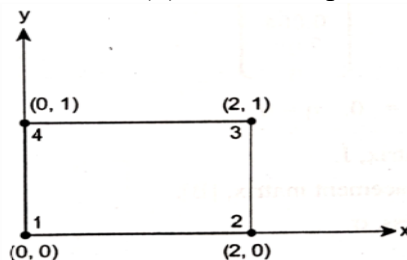


Figure-3

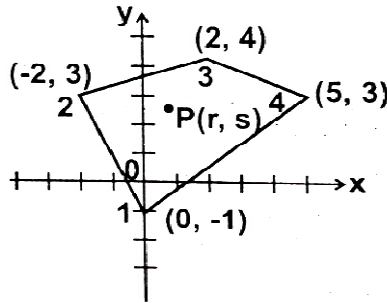
OR

- b) i) Evaluate the integral by applying 3-point Gaussian quadrature 6 K3 CO5

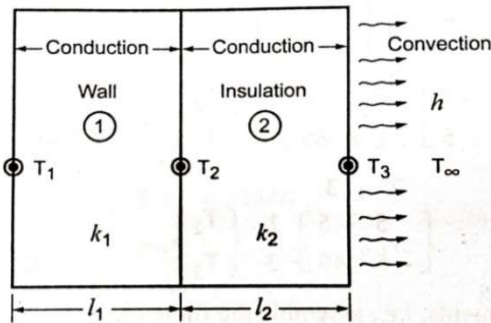
$$\int_{-1}^1 (x^4 + x^2) dx$$

- ii) The cartesian coordinates of the corner nodes of a quadrilateral elements are given by (0,-1), (-2,3), (2,4) and (5,3). Find the coordinates transformation between global and local co-ordinates. 7 K3 CO5

Using this, determine the cartesian co-ordinates of the point defined by $(r,s) = (0.5, 0.5)$ in the local co-ordinate system.



15. a) A wall of 0.6 m thickness having thermal conductivity of 1.2 W/mK. The wall is to be insulated with a material of thickness 0.06 m having an average thermal conductivity of 0.3 W/mK. The inner surface temperature is 1000°C and outside of the insulation is exposed to atmospheric air at 30°C with Heat transfer coefficient of $35\text{ W/m}^2\text{K}$. Calculate the nodal temperatures. 13 K3 CO6



OR

- b) Determine the first two natural frequencies of longitudinal vibration of the stepped steel bar shown in fig-4. All the dimensions are in m $E=30 \times 10^{10}\text{ N/m}^2$. and $\rho = 8500\text{ kg/m}^3$. 13 K3 CO6

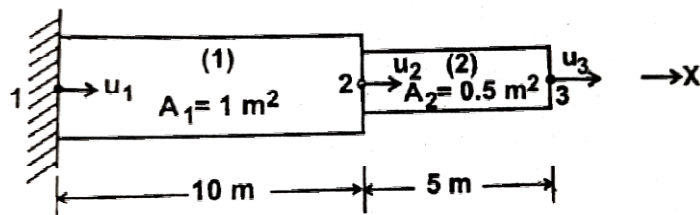


Figure-4

PART - C (1 × 15 = 15 Marks)

16. a) Determine the deflection at the centre of a simply supported beam subjected to uniformly distributed load over the entire span of length 'l' as shown in figure-5. Use Rayleigh Ritz method. 15 K3 CO4

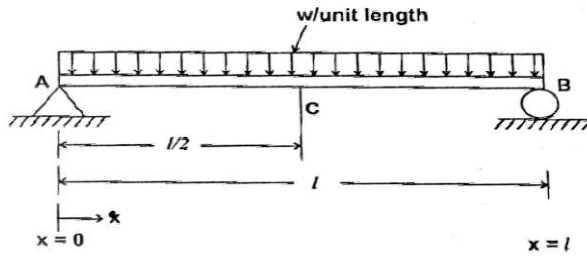


Figure-5.

OR

- b) For the tapered bar shown in figure-6 subjected to its own self weight, 15 K3 CO4 determine the deflection at the free end using Ritz Technique. Assume Youngs Modulus $E = 200 \text{ GPa}$ and density $\rho = 77 \text{ KN/m}^3$.

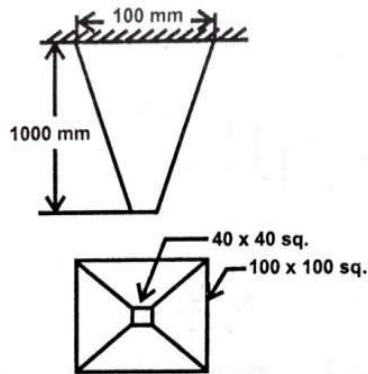


Figure-6.