



Question Paper Code

14203

B.E. / B.Tech. - DEGREE EXAMINATIONS, NOV / DEC 2025

First Semester

Civil Engineering

(Common to All Branches except CSBS)

24BSMA101 - MATRICES AND CALCULUS

Regulations - 2024

Duration: 3 Hours

Max. Marks: 100

PART - A (MCQ) (10 × 1 = 10 Marks)

Answer ALL Questions

	Marks	K-Level	CO
1. If A is orthogonal matrix, if (a) $A^T = A$ (b) $A^T = A^{-1}$ (c) $A=I$ (d) $AA^T=0$	1	K1	CO1
2. If A is real symmetric matrix, then its eigenvalues are (a) Always positive (b) Always real (c) Always imaginary (d) Always zero	1	K2	CO1
3. The necessary condition for maxima and minima of a function $f(x, y)$ is (a) $f_x = 0$ (b) $f_{yy} = 0$ (c) $f_x = 0$ and $f_y = 0$ (d) $f_{xx} = 0$	1	K1	CO2
4. If $x = r\cos\theta$ and $y = r\sin\theta$, then the Jacobian $\frac{\partial(x,y)}{\partial(r,\theta)}$ (a) -x (b) r (c) y (d) xy	1	K2	CO2
5. If $\nabla \cdot \vec{F} = 0$, the field is (a) Rotational (b) Divergent (c) Solenoidal (d) Irrotational	1	K1	CO3
6. Which theorem relates surface integral to volume integral? (a) Stoke's (b) Gauss divergence (c) Green's (d) Cauchy's	1	K1	CO3
7. In polar coordinate, then area element $dA=$ (a) $dx dy$ (b) $r dr d\theta$ (c) $dr d\theta$ (d) $xy dx dy$	1	K1	CO4
8. The Divergence theorem relates which two types of integrals (a) Line and surface (b) surface and volumr (c) line and volume (d) scalar and vector	1	K1	CO4
9. Triple integrals are used to find (a) Gradient (b) Curve length (c) Area (d) Volume	1	K1	CO5
10. Parseval's theorem gives a relation between (a) Time and frquency domain energies (b) Amplitude and phase (c) Area (d) None	1	K1	CO6

PART - B (12 × 2 = 24 Marks)

Answer ALL Questions

11. If the matrix $A = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 4 \end{bmatrix}$ find the eigenvalues of A^2 .	2	K2	CO1
12. State Cayley Hamilton Theorem.	2	K1	CO1
13. Find the stationary points of the function $f(x, y) = x^3 + y^3 - 12x - 3y + 20$.	2	K2	CO2
14. If $u = x + y$, $v = x - y$ evaluate the jacobian of $\frac{\partial(u,v)}{\partial(x,y)}$.	2	K2	CO2
15. Find 'a' such that $(3x - 2y + z)\vec{i} + (4x + ay - z)\vec{j} + (x - y + 2z)\vec{k}$ is solenoidal.	2	K2	CO3

16. Prove that $\nabla \times \vec{r} = 0$. 2 K2 CO3
17. State Stoke's theorem. 2 K1 CO4
18. If $\vec{F} = x^2\vec{i} + xy^2\vec{j}$, evaluate the line integral $\int_C \vec{F} \cdot d\vec{r}$ from (0,0) to (1,1) along the path $y=x$. 2 K2 CO4
19. Evaluate $\int_0^1 \int_1^2 x(x+y) dydx$. 2 K2 CO5
20. Evaluate $\int_0^1 \int_0^2 \int_0^3 xyzdzdydx$. 2 K2 CO5
21. State Dirichlet's conditions. 2 K1 CO6
22. Find b_n in the expansion of x^2 as a Fourier Series in $(-\pi, \pi)$. 2 K2 CO6

PART - C (6 × 11 = 66 Marks)

Answer ALL Questions

23. a) Verify Cayley -Hamilton theorem for $A = \begin{bmatrix} 1 & 0 & 3 \\ 2 & 1 & -1 \\ 1 & -1 & 1 \end{bmatrix}$ and hence find A^{-1} . 11 K3 CO1

OR

- b) Reduce the quadratic form $x^2 + y^2 + z^2 - 2xy - 2yz - 2zx$ to canonical form through an orthogonal transformation. 11 K3 CO1
24. a) Expand $e^x \cos y$ about $(0, \frac{\pi}{2})$ up to the third term using Taylor's series. 11 K3 CO2

OR

- b) A rectangular box open at the top, is to have a volume of 32 cc. Find the dimensions of the box, that requires the least material for its construction. 11 K3 CO2
25. a) Show that $\vec{F} = (6xy + z^3)\vec{i} + (3x^2 - z)\vec{j} + (3xz^2 - y)\vec{k}$ is irrotational vector and find the scalar potential function. 11 K3 CO3

OR

- b) Show that $r^n \vec{r}$ is an irrotational vector for any value of n but is solenoidal only if $n = -3$. 11 K3 CO3
26. a) Using Green's theorem evaluate $\int_C \{(xy + y^2)dx + x^2dy\}$, where C is the closed region bounded by $y=x$ and $y = x^2$. 11 K3 CO4

OR

- b) Verify divergence theorem for $\vec{F} = x^2 \vec{i} + z \vec{j} + yz \vec{k}$ over the cube formed by the plane $x=0, x=1, y=0, y=1, z=0, z=1$. 11 K3 CO4
27. a) Change the order of integration and hence evaluate $\int_0^{4a} \int_{\frac{x^2}{4a}}^{2\sqrt{ax}} dydx$. 11 K3 CO5

OR

- b) Find the volume of the ellipsoid $\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} = 1$ by using triple integrals. 11 K3 CO5
28. a) Find the Fourier series of the function $f(x) = x^2$ in the interval $(0, 2\pi)$. 11 K3 CO6

OR

- b) Find the cosine series for $f(x) = x$ in $(0, \pi)$ and then using Parseval's theorem. Hence show that $1 + \frac{1}{3^4} + \frac{1}{5^4} + \dots = \frac{\pi^4}{96}$. 11 K3 CO6

