

9. Which famous problem is often used as the first problem to be proven NP-Complete? 1 K1 CO5
 (a) Traveling Salesperson Problem (TSP) (b) Matrix-Chain Multiplication
 (c) Satisfiability Problem (SAT) (d) Shortest Path Problem
10. A problem is in the complexity class P if it can be solved by a deterministic Turing machine in: 1 K1 CO6
 (a) Exponential time. (b) Polynomial time. (c) Logarithmic time. (d) Factorial time.

PART - B (12 × 2 = 24 Marks)

Answer ALL Questions

11. Compare between the Big O and Big Ω notations. 2 K2 CO1
12. What is the primary difference in the operational principle between the Substitution Method and the Recursion-Tree Method for solving recurrences? 2 K1 CO1
13. Show the Red-Black Tree Property related to the color of the root and the leaves (NIL nodes). 2 K2 CO2
14. Define the minimum degree (t) of a B-Tree. 2 K1 CO2
15. When is Breadth-First Search (BFS) preferred over Depth-First Search (DFS) in graph traversal? 2 K1 CO3
16. Explain the purpose of the relax operation in the context of single-source shortest path algorithms. 2 K2 CO3
17. What are the two key components that a problem must exhibit to be efficiently solved using Dynamic Programming? 2 K1 CO4
18. Compare between a Greedy Algorithm and a Dynamic Programming algorithm. 2 K2 CO4
19. Interpret the recurrence relation for LCS. 2 K2 CO5
20. Infer any two real-life applications of greedy algorithms. 2 K2 CO5
21. Explain in detail about NP complete problem with an example. 2 K2 CO6
22. Compare NP Completeness and NP Hard. 2 K2 CO6

PART - C (6 × 11 = 66 Marks)

Answer ALL Questions

23. a) Apply an algorithm for Insertion Sort and analyze its worst-case time complexity using O-notation. 11 K3 CO1
- OR**
- b) Make use of the Recursion-Tree Method to determine the asymptotic bound for the recurrence $T(n)=3T(n/2)+O(n)$. 11 K3 CO1
24. a) Analyze the process of Insertion into a Red-Black Tree. Clearly describe the scenarios that require rotations and color changes to maintain the properties. 11 K4 CO2
- OR**
- b) Examine the structure of a Fibonacci Heap and explain the efficient Mergeable-heap operation UNION(H1,H2). 11 K4 CO2
25. a) Explain the steps of Dijkstra's Algorithm. Trace its execution on a small weighted, directed graph to find the shortest paths from a source vertex S. 11 K2 CO3
- OR**
- b) Compare and contrast Kruskal's Algorithm and Prim's Algorithm for finding the Minimum Spanning Tree (MST), focusing on the data structures they typically use and how they "grow" the tree. 11 K2 CO3
26. a) Apply the concept of Single-Source Shortest Path (SSSP) algorithm for Directed Acyclic Graphs (DAGs) and also analysis of time complexity. 11 K3 CO4

OR

- b) Apply the Greedy Strategy and apply it to construct Huffman Codes for a set of 11 K3 CO4 characters with given frequencies.
27. a) Explain the Matrix Chain Multiplication problem using dynamic programming for 11 K2 CO5 the following.
a) Derive the recurrence relation.
b) Construct the cost table for the sequence: A1(10×30), A2(30×5), A3(5×60).
c) Find the minimum number of scalar multiplications.
- OR**
- b) Explain the Fractional Knapsack problem using the greedy method with an 11 K2 CO5 example.
28. a) Construct the Travelling Salesman Problem and prove that it is NP-Complete. 11 K3 CO6
- OR**
- b) Apply the concept of NP-Completeness to a real-world computational problem like 11 K3 CO6 job scheduling, resource allocation etc.