

19. Define Fourier Transform pair.	2	K1	CO4
20. State and prove change of scale property on Fourier transforms.	2	K2	CO4
21. Find $Z[na^n]$.	2	K1	CO5
22. State convolution theorem on Z-transform.	2	K1	CO5

PART - C (6 × 11 = 66 Marks)

Answer ALL Questions

23. a)	Show that $F^n = \{(a_1, a_2, \dots, a_n) : a_i \in F\}$ is a vector space over F with respect to addition and scalar multiplication defined component wise.	11	K3	CO1
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OR

b)	Check whether $2x^3 - 2x^2 + 12x - 6$ is a linear combination of $x^3 - 2x^2 - 5x - 3$ and $3x^3 - 5x^2 - 4x - 9$.	11	K3	CO1
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24. a)	Find an orthonormal basis of the inner product space $R^3(R)$ with standard inner product, given the basis $B = \{(1, 1, 0), (1, -1, 1), (-1, 1, 2)\}$ using Gram-Schmidt orthogonalization process.	11	K3	CO2
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OR

b)	Let $T: R^2 \rightarrow R^3$ be defined by $T(x, y) = (x + 3y, 0, 2x - 4y)$. Compute the matrix of the transformation with respect to the standard basis of R^2 and R^3 . Find $N(T)$ and $R(T)$.	11	K3	CO2
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25. a)	Solve the following equation $(D^2 + 2DD' + D'^2)z = e^{x-y} + xy$.	11	K3	CO3
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OR

b)	Solve the equation $x(y - z)p + y(z - x)q = z(x - y)$.	11	K3	CO3
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26. a)	Find the Fourier transform of $f(x)$ given by $f(x) = \begin{cases} a^2 - x^2; & x < a \\ 0; & x > a > 0 \end{cases}$ Hence prove that $\int_0^\infty \frac{\sin x - x \cos x}{x^3} dx = \frac{\pi}{4}$.	11	K3	CO4
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OR

b)	Apply Fourier transform to find the value of $\int_0^\infty \frac{dx}{(x^2 + a^2)(x^2 + b^2)}$.	11	K3	CO4
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27. a)	Apply convolution theorem to find inverse Z-transform of $\frac{8z^2}{(2z-1)(4z-1)}$.	11	K3	CO5
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OR

b)	Solve $u_{n+2} + 4u_{n+1} + 3u_n = 3^n$ given that $u_0 = 0, u_1 = 1$ using the Z transform.	11	K3	CO5
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28. a) (i)	Find the basis for the subspace $W_2 = \{(a_1, a_2, a_3, a_4, a_5) \in F^5 / a_2 = a_3 = a_4 \text{ and } a_1 + a_5 = 0\}$ of F and hence find dimension of W_2 .	6	K3	CO1
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(ii)	Let $V = P(R)$, the vector space of polynomials over R with inner product defined	5	K3	CO2
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by $\langle f, g \rangle = \int_0^1 f(t)g(t)dt$, where $f(t) = t + 2$, $g(t) = t^2 - 2t - 3$.

Find $\|f\|$ and $\|g\|$.

OR

b) (i)	Determine if the set $\{x^3 + 2x^2, -x^2 + 3x + 1, x^3 - x^2 + 2x - 1\}$ is linearly dependent or linearly independent in $R^3(R)$.	6	K3	CO1
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(ii)	Let $T: R^3 \rightarrow R^2$ be defined by $T(x, y, z) = (2x - y, 3z)$. Verify whether T is linear or not. Also find $N(T)$.	5	K3	CO2
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